Evaluation of Lightning Multiple Strokes Nature on Aircraft Avionic Equipment Performance Based on TLM

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Abstract

The phenomenon of lightning is a highly intricate natural occurrence characterized by the rapid discharge of electricity in the atmosphere. Understanding the intricacies of lightning encompasses a range of scientific disciplines, including meteorology, physics, power engineering, and environmental science. Lightning inductive effects can result in undesired operation of the avionic equipment and endanger flight safety. This paper analyses the multiple-stroke nature of an actual flash for evaluating the indirect effects properly such as coupling into the interior equipment of an aerospace vehicle. To the best of our knowledge, subsequent strokes in the flash tend to have a higher rate of rise and lower crest amplitudes, compared to the initial stroke. The metallic aircraft structure acts as a full Faraday cage, while composite materials can decrease the electromagnetic shielding efficiency of the original metal body. The time domain finite element analysis based on the transmission line model method is regarded as a numerical technique to solve field problems by implementing circuit equivalents. The objective of this study is to examine the characteristics associated with lightning strikes by the MIL-STD-464A standard. It also aimed to simulate the induced current in coaxial cables, surface current density, and electric and magnetic field strength by integrating Matlab and CST software.

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Keywords: lightning, Subsequent strokes, avionic, composite, Coaxial cable

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AUT Journal of Electrical Engineering 10.22060/EEJ.2025.23758.5633

1. Introduction

Aircraft flight safety can be affected by various atmospheric disturbances, with lightning being one of the most significant. Lightning is a natural electrical discharge that typically occurs within cumulonimbus clouds during precipitation. It can adversely affect aircraft systems and equipment, leading to malfunctions, failures, or incorrect data readings. Lightning strikes pose both direct and indirect threats. Direct effects include physical damage such as pitting, melting of aircraft surfaces, and the ignition of fuel vapors [1]–[6]. Indirect effects involve electromagnetic interference with avionics, navigation systems, and other onboard electronic equipment [7]–[11]. The vulnerability of electronic systems has increased with advancements in semiconductor technology, particularly the reduction in the size of semiconductor junctions, which makes them more susceptible to electrostatic damage [12]. Smaller semiconductor junctions are exposed to some damage from electrostatic voltages. One industry that has been significantly impacted by the erratic weather patterns resulting from climate change and global warming is aviation. Climate change and global warming now have an increasing impact on weather-related aircraft accidents[13]. Lightning not only threatens aircraft in flight but also poses risks to airport operations and air traffic control (ATC) systems [14].

2. Significance of lightning certification

According to MIL-STD-464A [15], aircraft will meet its operational performance requirements for both direct and indirect effects of lightning. The expression of the double exponential model of the lightning current is as follows:

$$i(t) = I_0 \left\{ \exp\left(\frac{-t}{\alpha}\right) - \exp\left(\frac{-t}{\beta}\right) \right\}$$
(1)

Where i(t) represents the instantaneous value of lightning current, I_0 indicates the peak value of lightning, α shows decay time, and β is considered as rise time. Table 1 presents standard parameters for lightning currents, where a typical lightning flash consists of an initial return stroke followed by several subsequent strokes.

		I(t)			
Current component	Description	lightning's peak value(A)	decay time(s)	rise time(s)	
Α	Severe stroke	218810	88e-6	1.5e-6	
В	Intermediate current	11300	14e-4	5e-4	
С	Continuing current	400 for 0.5s	Not applicable	Not applicable	
D	Restrike	109405	44e-6	7.7e-7	
D/2	Multiple stroke	54703	44e-6	7.7e-7	
Н	Multiple burst	10572	5.3e-6	5.23e-8	

Table 1.	Lightning	current	based	on	Mil-	Std-4	-64A

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For protection against direct effects, a single return stroke is usually sufficient, but for assessing indirect effects, such as electromagnetic coupling in aerospace vehicles, multiple strokes must be considered, as discussed in references [15]–[17]. One can use Fig. 1 to evaluate the indirect effects of the lightning environment..



Fig. 1. The indirect effects of lightning on the environment [15]. (a) Multiple stroke waveforms. (b) Multiple burst waveforms

The first return stroke is typically modeled using a double exponential function. For subsequent strokes, the Heidler function [18] is preferred due to its more accurate and flexible representation of the waveform characteristics, making it ideal for simulating lightning surges:

$$I(0,t) = \frac{I_p}{k} * \left\{ \left(\frac{t}{T_f}\right)^n / 1 + \left(\frac{t}{T_f}\right)^n \right\} * \exp\left(\frac{-t}{t_{au}}\right)$$
(2)

Where Ip is the peak current; k is the correction factor for the peak current; t is the time; Tf is the front time constant; tau is the tail time constant and n is the current steepness factor. Transient phenomena can be classified into various groups:

- 1- Temporary overvoltage transients are low-frequency transients in the range of 0.1Hz to 3 KHz
- 2- The switching transients class are slow front surges in the range of 60Hz to 20KHz
- 3- Lightning class is a fast transient in the range of 10 KHz to 3MHz
- 4- Restrike overvoltage is very fast front surges in the range of 10 KHz to 50MHz

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Fig. 2 displays the classification of lightning entry and exit points[19]. The present study focuses on Route 1.



Fig. 2. Entry and exit points of the lightning strike on an aircraft

3. Simulation of lightning

It is important to clarify that lightning is inherently a random phenomenon due to the unpredictability of its time, location, and intensity. These characteristics make lightning events difficult to model deterministically. However, for the purpose of design and simulation, particularly in aerospace contexts, deterministic models are often employed to facilitate more controlled and reproducible conditions. In our manuscript, we refer to MIL-STD-464A, a standard for lightning protection in aircraft, which provides specific lightning current waveform models. In order to evaluate the indirect effects of lightning, the number of multiple strokes usually ranges from 1-24, with a mean value of 3. Subsequent strokes in the flash tend to have a higher rate of rise and lower peak amplitudes, compared to the initial stroke. Thus, they can play a significant role in inducing voltages in aircraft wiring. To simulate lightning current and analyze the data, Matlab software was used to focus on subsequent strokes. The simulated waveform includes an initial stroke, three sections of multiple-stroke

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waveforms, and three sections of multiple-burst waveforms. Fig. 3 represents a simulated waveform in which the frequency

ranges from 10 kHz to 3MHz.



Simulated Aircraft lightning Strike

Fig. 3. Waveform of lightning current to evaluate the indirect Effects

4. Numerical instrument

4.1. Introduction of Microstripe module

CST Microstripe is the ultimate 3D electromagnetic simulation software that employs the advanced time-domain Transmission Line Matrix (TLM) method to provide unparalleled accuracy and efficiency. This module is appropriate for structures that can function in the range with high frequency. The "Compact modeling" technique is implemented to demonstrate coupling through apertures, panels, and interaction with cabling efficiently. The Microstripe module delivers extraordinary performance for their use in the real world. A powerful Octree-based meshing algorithm represents the model details accurately, although it can decrease the cell count totally by integrating cells in less critical regions, which may lead to a more than 90% decrease in cell count, compared to basic graded-mesh techniques[20].

4.2. TLM method

The transmission line matrix method is regarded as a numerical technique to solve field problems by implementing circuit equivalents. This method is based on the equivalence between Maxwell's equations and those related to voltages and currents on a mesh of continuous two-wire transmission lines. The simplicity of formulation and programming for a wide range of applications is regarded as the main characteristic of this method. TLM method is considered a discretization

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process similar to other numerical techniques. Unlike mathematical discretization approaches such as finite difference and

finite element methods, TLM is considered a physical discretization approach[21], [22].

Fig. 4 illustrates a schematic plan of the solution of a problem by transmission line method.



Fig. 4. Solution steps of a problem by TLM [18].

As shown in Fig. 5, the symmetrical condensed node is considered as the structure used for node substitution.



Fig. 5. Structure of SCN model [23]

The equations governing the voltage and current behavior at each node are represented by the following differential equations [24], [25]:

$$v \frac{\partial I_{z}}{\partial y} - w \frac{\partial I_{y}}{\partial z} = 2C_{x} \frac{\partial V_{x}}{\partial t} , \qquad v \frac{\partial V_{z}}{\partial y} - w \frac{\partial V_{y}}{\partial z} = -2L_{x} \frac{\partial I_{x}}{\partial t}$$

$$w \frac{\partial I_{x}}{\partial z} - u \frac{\partial I_{z}}{\partial x} = 2C_{y} \frac{\partial V_{y}}{\partial t} , \qquad w \frac{\partial V_{x}}{\partial z} - u \frac{\partial V_{z}}{\partial x} = -2L_{y} \frac{\partial I_{y}}{\partial t}$$

$$u \frac{\partial I_{y}}{\partial x} - v \frac{\partial I_{x}}{\partial y} = 2C_{z} \frac{\partial V_{z}}{\partial t} , \qquad u \frac{\partial V_{y}}{\partial x} - v \frac{\partial V_{x}}{\partial y} = -2L_{z} \frac{\partial I_{z}}{\partial t}$$

$$(3)$$

In this context, u, v, and w represent the node dimensions along the x, y, and z axes, respectively. The inductances (Lx, Ly, Lz) and capacitances (Cx, Cy, Cz) of the transmission lines in the x, y, and z directions are considered. The currents (Ix, Iy,

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Iz) and voltages (Vx, Vy, Vz) correspond to the transmission lines along these axes. The relationship between the voltages,

currents, and the electromagnetic fields in the solution domain can be described as follows:

$$H_{x} = \frac{I_{x}}{u} , \qquad E_{x} = \frac{-V_{x}}{u}$$

$$H_{y} = \frac{I_{y}}{v} , \qquad E_{y} = \frac{-V_{y}}{v}$$

$$H_{z} = \frac{I_{z}}{w} , \qquad E_{z} = \frac{-V_{z}}{w}$$
(4)

Eq. (5) is derived by substituting Eq. (3) into Eq. (4):

$$\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} = C_x \frac{2u}{wv} \frac{\partial E_x}{\partial t} , \qquad \frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} = -L_x \frac{2u}{wv} \frac{\partial H_x}{\partial t}$$

$$\frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x} = C_y \frac{2v}{uw} \frac{\partial E_y}{\partial t} , \qquad \frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x} = -L_y \frac{2v}{uw} \frac{\partial H_y}{\partial t}$$

$$\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} = C_z \frac{2w}{uv} \frac{\partial E_z}{\partial t} , \qquad \frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -L_z \frac{2w}{uv} \frac{\partial H_z}{\partial t}$$
(5)

As a result, it transforms into the following equation:

$$\begin{cases} \nabla \times E = -\mu \frac{\partial H}{\partial t} \\ \nabla \times H = \varepsilon \frac{\partial E}{\partial t} \end{cases}$$
(6)

The scattering and connection processes are iteratively performed until they are suitable for simulating propagation over any desired time interval. During this process, voltages and currents are available at each stage. Additionally, these values represent the electromagnetic fields associated with the specific configuration and excitation of the problem at hand. The output is directly linked to the time domain.

5. Geometry of fuselage

In this study, the fuselage geometry is modeled based on the Airbus A320 aircraft, which features 80 windows (40 on each side). The aircraft has a total length L = 37.6 m, a wingspan W = 34 m, and an overall height H = 11.8 m. Each window has a dimension of 0.2 m x 0.3 m, as illustrated in Fig. 6. A major computational challenge arises from the disparity in structural scales: the aircraft length is 37.6 m, while the composite skin thickness is approximately 1 mm. This leads to a scale ratio of approximately L/t = 37,600, which causes numerical stiffness in traditional finite-element or finite-difference time-domain (FDTD) solvers. This issue has been addressed in previous studies[26], [27]. To manage this, CST Microwave Studio employs the compact model technique, which allows for the simplification of thin structures (such

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as skins or coatings) into surface impedance boundary conditions (SIBC). This approach reduces the mesh density required in the thickness direction without sacrificing accuracy. The skin depth and surface impedance of a good conductor at high frequencies are approximately given by [20]:

$$\boldsymbol{\delta} = \sqrt{\frac{2}{\omega\mu\sigma}} \quad , \quad \boldsymbol{Z}_{s} = \left(\frac{1}{\sigma\delta}\right)\left(1+j\right) \tag{7}$$

where δ is the skin depth, Z_s is the surface impedance, σ is the conductivity μ is the magnetic permeability of the material, and $\omega = 2\pi f$ is the angular frequency. This treatment allows the simulation to remain computationally feasible while maintaining fidelity to the physical behavior of EM wave propagation and attenuation through and around structural features such as windows.



Fig. 6. Modeled aircraft in Simulator

Table 2 indicates the simulation of aluminum and carbon fiber as the fuselage types in the aircraft [28].

Table 2. P	Table 2. Properties of aircraft fuselages			
Properties	Carbon Fiber	Aluminum		
Relative permittivity	12	1		
Relative permeability	1	1		
Electric conductivity	29300 in longitudinal	3.54e+007		
(S/m)				
Thickness	1mm	1mm		

Table 2. Properties of aircraft fuselages

Coaxial cables, RG174, and RG-optional are evaluated as shielded cables. As shown in Table 3, the shielding properties of the cable are determined by using a transfer impedance model. Kley's formula is used for calculating the transfer impedance [29]–[33]:

$$Z_T = Z_R + i\,\omega L_T + (1+i)\,\omega L_S \tag{8}$$

Where Z_T is the transfer impedance of a single braided shield, Z_R is the Transfer impedance of an equivalent tube, L_T is the coupling inductance and L_S is the skin inductance.

This formulation models the coupling mechanism with respect to the field penetration through the shield apertures. As illustrated in Fig. 7, the basic components of a coaxial cable, from the inside out, are the center conductor, dielectric, one or more shield layers, and an outer jacket. The cost of manufacturing coaxial cables is significantly impacted by the outer conductor or shield. RG 174 and RG-optional are terminated at 50 ohms.

rable 5. Cable parameters				
Specifications	Shielded cable	Shielded cable		
	RG 174	(optional)		
Inner wire diameter(mm)	0.48	0.48		
Braid diameter(mm)	1.93	1.93		
Filament diameter(mm)	0.1	0.05		
Number of filaments in one	5	4		
carrier				
Number of carriers	16	8		
Transfer resistance(Ω/m)	0.0327191	0.3391833		
Transfer inductance(H/m)	5.99e-10	4.4015e-8		



Fig. 7. Coaxial cable components

In order to measure surface current, electric field strength, and magnetic field strength, three probes are defined at various locations as shown in Table 4.

Table 4. Coordinates of probes				
Coordinate (x, y, z) in m				
(22, 0.5, 0)				
(22, 2.95, 0)				
C- Outside aircraft (22, 3.5, 0)				

7.1. Surface current distribution on aircraft skin

Transient surface current on aluminum and carbon fiber composite (CFC) skins is illustrated in Fig. 8. As shown, surface current density at the lightning entry and exit points is significantly higher than other regions due to the electromagnetic boundary conditions:

$$J_s = \hat{n} \times (H_2 - H_1) \tag{9}$$

Where Js is the surface current density, \hat{n} is the unit normal pointing from medium1 to medium2, and H₁ and H₂ are the magnetic field intensities just below and above the surface. This relationship follows directly from Maxwell's equations and surface boundary conditions[34].



Fig. 8. Expansion of surface current: a) CFC skin, and b) AL skin.

When a lightning channel attaches to an aluminum skin, localized melting can occur at the strike point. For CFC, however, resistive heating has an entirely different effect at entry and exit points. The damage may lead to a puncture. While aluminum can bend without breaking, CFC materials are rigid and prone to crushing. This damage is usually limited to the adjacency of the lightning attachment point. The aluminum model does not experience any significant temperature rise and remains almost near the ambient temperature.

7.2. Magnetic and electric field strength

Electric and magnetic field strengths are measured at three probes, A, B and C. The results in the time domain and frequency domain are displayed in Fig. 9 and Fig.10, as well as in Table 5 and Table 6.

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Fig. 9. Electric field strength in the time domain: a) AL, and b) CFC.



Fig.10. Magnetic field strength in time and frequency domain: a) AL, and b) CFC.

Tuote 5. Electric field Strengtin.		
Case	CFC	Aluminum
Probe A	487V/m	5.9V/m
Probe B	553V/m	9.6V/m
Probe C	8.1MV/m	8.1MV/m
Shielding effectiveness	84.4 dB	122.7 dB
(SE _E)		

Table 5	. Electric	field	strength.
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Table 5 and Table 6 indicate the calculation of the shielding effectiveness of the aircraft skin. The shielding effectiveness

is defined as the ratio of a field magnitude without the shield in place to the field magnitude with the shield in place.

Table 6. Magnetic field strength			
Case	CFC	Aluminum	
Probe A	150.4A/m	527mA/m	
Probe B	1.1KA/m	1.94A/m	
Probe C	5.16KA/m	4.5KA/m	
Shielding effectiveness	30.7 dB	78.6 dB	
(SE _M)			

The shielding effectiveness of electric and magnetic fields in dB is defined as follows:

$$SE_{E} = 20 log \left| \frac{E_{outside}}{E_{transmitted}} \right|$$

$$SE_{M} = 20 log \left| \frac{H_{outside}}{H_{transmitted}} \right|$$
(10)
(11)

As presented in Tables 5 and 6, the shielding effectiveness of the aluminum skin is significantly superior to that of the CFC skin.

7.3. Induced current in coaxial cable

The induced current in coaxial cables is presented in Fig. 11. The peak induced current is shown in Table 7.

Coaxial cables		Peak induced current		
		Aluminum skin	CFC skin	
RG 174	Shield screen	9.9 mA	13.3 A	
	Inside wire	23.9 uA	32.2 mA	
Shielding effectiveness(dB)		52.3	dB	

 Table 7. Peak values of induced current in coaxial cables

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RG-optional	Shield screen	9.6 mA	13 A
	Inside wire	236.3 uA	320 mA
	Shielding effectiveness(dB)	32.2 dB	



Fig. 11. Induced current signal inside wire: a) RG174, b) RG-Optional

As shown, the peak values of induced current in the inner wire of RG174 are lower than those in RG-optional. The shielding effectiveness of RG174 is 52.28 dB, while the RG-optional is 34.3 dB. It is worth noting that the protection offered by Aluminum skin is significantly superior to that of CFC skin.

AUT Journal of Electrical Engineering 10.22060/EEJ.2025.23758.5633 8. Conclusion

This study quantified how the multi-stroke nature of a lightning flash affects the electromagnetic protection of aircraft. A full-wave TLM solver, enhanced with compact model surface impedance boundary conditions, was integrated with multistroke current waveforms generated in MATLAB that comply with MIL-STD-464A. The numerical methods of the electromagnetic effects such as TLM have the advantage of higher flexibility and lower costs with respect to the experimental approach. High investment and high-risk characteristics of experimental tests may cause a lot of inconvenience. Therefore, conducting the simulation of lightning protection is essential. The induced current, surface current density, and electric and magnetic field strengths were analyzed by comparing aluminum and composite fuselage structures. The present study could guarantee how much shielding is needed to achieve the best trade-off between minimization of weight and lightning-induced effects inside the aircraft. Finally, adding excessive shielding to the cable harnesses significantly increases the weight and reduces the routing flexibility. Although aluminum fuselage structures provide certain advantages in electromagnetic protection compared to carbon fiber composites (CFC), CFC materials are often preferred in contemporary aircraft design due to their superior strength-to-weight ratio. Consequently, CFC has become increasingly prevalent in modern aviation, despite the additional challenges it poses in terms of lightning protection. Results indicate that relying solely on single-stroke tests for certification is insufficient. Implementing conductive coatings, low-transfer-impedance cable shielding, and optimized cable routing are key strategies to ensure the reliability of avionics systems in modern fleets.

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