

# Vertical Tunneling Transistor Based on Gr-hBN- $\chi_3$ Borophene Heterostructure with AA Stack

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**ABSTRACT:** In this paper, the electronic properties of vertical Gr-hBN- $\chi_3$  borophene heterostructure (AA stack between Gr and hBN layers), i.e., (Gr-hBN- $\chi_3$ \_AA), have been investigated by density functional theory (DFT). By using the tight-binding (TB) model and least-square fitting for TB and DFT band structures, optimal TB parameters are calculated. By exploiting the non-equilibrium Green function technique and capacitive model, we have investigated the vertical tunneling transistor (VTFET) based on Gr-hBN- $\chi_3$ \_AA. Also, the figure of merit (FOM) of the device, such as the  $I_{ON}/I_{OFF}$  ratio, subthreshold swing, and intrinsic gate-delay time, has been extracted. We have concluded that decreasing the width of the graphene nanoribbon improves the switching ratio, subthreshold swing, and gate-delay time. Also, compared to previous work (VTFET based on Gr-hBN- $\chi_3$ \_AB), it is seen that changing the stack between Gr and hBN layers has little effect on the FOM of the device. The gate-delay time of the device is 0.011 ps at room temperature.

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## 1- Introduction

The fast growth of information technology (IT) has been sustained by the continuous scaling down of the transistor dimensions. In the last decade, on the one hand, two-dimensional (2D) [1], transition-metal-dichalcogenides (TMD) [2], and metallic-transition-metal-dichalcogenides (MTMDs) [3] and on the other hand, innovative structures [4], have played an important role in this regard. One of these innovative structures is a vertical heterostructure. Vertical structures with van der Waals (vdW) bonds between layers are promising to reduce the size and energy consumption of the device and keep Moore's law stable [5-8]. However, those suffering from a lattice mismatch and displacement of layers [9]. Nevertheless, IBM and SAMSUNG companies have introduced a new vertical tunneling transistor (VTFET) to help sustain Moore's law for years to come [10].

In 2012, the first VTFET based on Gr-hBN(MoS<sub>2</sub>)-Gr heterostructures was proposed and fabricated [11]. In the last decade, VTFETs based on Gr-hBCN [12], Gr-TMD [13], II-type heterostructure [14], and 3D-2D heterostructures [15] have been investigated. Also, VTFETs with metallic drain have been presented as follows. In 2013, Yu et al. experimentally investigated a VTFET based on Gr-MoS<sub>2</sub>-Ti heterostructure [16]. In 2021, Lee et al. [17] (Liu et al. [18]) reported a VTFET based on Gr-hBN-metal (Gr-MoS<sub>2</sub>-Ag) heterostructure. In 2022, Abbasi et al. theoretically proposed

and investigated another VTFET based on Gr-hBN- $\chi_3$  borophene heterostructure [19]. However, VTFETs have the potential to be designed and fabricated with sub-1-nm gate length [20].

In this work, we numerically simulate a tunneling transistor based on a vertical Gr-hBN- $\chi_3$  borophene heterostructure (AA stack between Gr and hBN layers), i.e., (Gr-hBN- $\chi_3$ \_AA). We have investigated the effect of changing the stack between Gr and hBN layers compared to the reference [19].

Borophene is a 2D material with different phases that was first realized on the silver crystal substrate by the MBE system [21, 22]. This material has unique physical, chemical, and optical properties and could be a candidate for the next generation of electronics [23-26]. However, so far, its instability has limited its large-scale applications. Meanwhile, the three main structures of borophene are  $\chi_3$ ,  $\beta$ , and striped borophene [21, 22]. Also, new phases of borophene, such as the glass state of borophene, liquid borophene, and borophene with large holes, have been discovered [27]. The  $\chi_3$  borophene has metallic properties [28]. In this work, it has been used in the drain of the device.

We exploited the non-equilibrium Green Function (NEGF) formalism combined with the tight-binding (TB) and capacitive models to calculate the electrical characteristics of VTGr $\chi_3$  FET (AA stack between Gr and hBN layers). The article's organization is as follows: Section 2 describes the energy band diagram of the device. The first-principle results, TB model, and NEGF are presented in Section 3. Section 4

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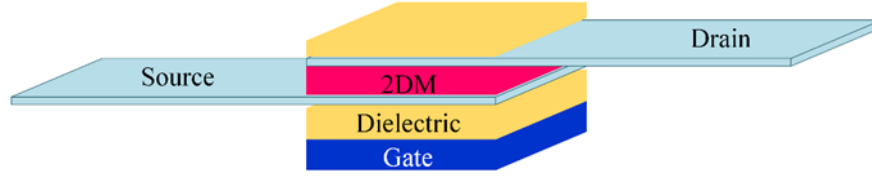


Fig. 1. Apparent schematic of the device.

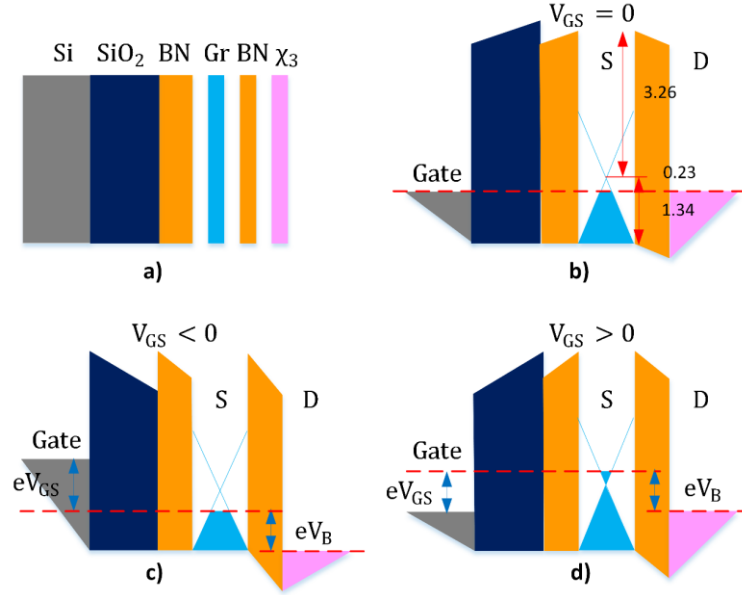


Fig. 2. (a) Schematic of VTGr $\chi_3$ FET. Band diagram corresponding to (b) No bias, (c) ON state, and (d) OFF state.

discusses the results. Finally, the conclusion is expressed in 5.

## 2- Device structure and Operational principle

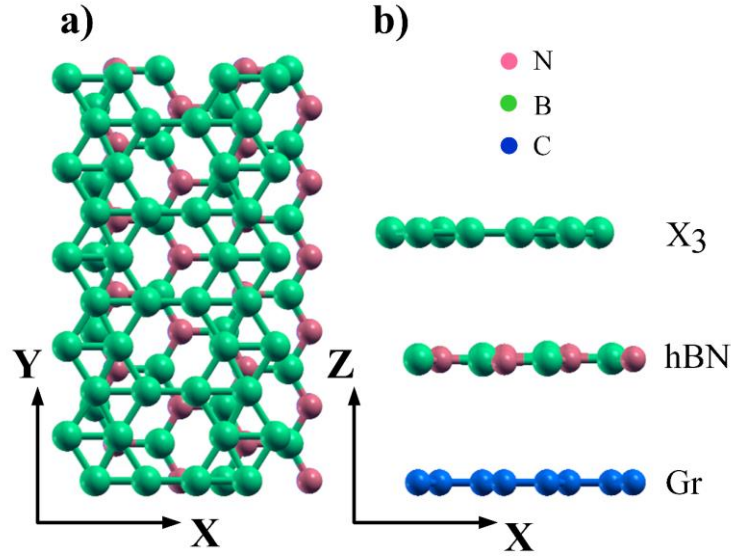
Fig. 1 shows the apparent schematic of the device with two contacts. Fig. 2(a) presents a cross-sectional view of the physical structure and band alignment of the device. The source (drain) in the device is graphene ( $\chi_3$  borophene). Those are electrically separated by one layer of hBN barrier. The gate oxide is  $\text{SiO}_2$ , and a layer of hBN is exfoliated on it [11]. The stack type between graphene and hBN layers is assumed AA. Fig. 2(b) illustrates the band diagram of the VTGr $\chi_3$  FET in zero bias. For  $V_{GS} < 0$ , the Fermi level shifts downwards, reducing the effective height of the tunneling barrier, which represents the ON state (Fig. 2(c)), whilst the Fermi level shifts upwards by applying a  $V_{GS} > 0$ , therefore the effective height of the tunneling barrier increases, which shows the OFF state in Fig. 2(d). The voltage between the graphene and  $\chi_3$  borophene sheets ( $V_B$ ) controls the tunneling current. This structure uses graphene's low density of states (DOS) feature. As shown in Fig. 2, the DOS of graphene and  $\chi_3$  borophene and the effective height of the barriers are modified by varying the gate-source voltage. Hence, the current is modulated. The

device's manufacturing process can be similar to VTFET based on Gr-hBN-Gr heterostructure [11].

## 3- Band Structure and Modeling

### A. First principle calculation

To discover the electronic properties of Gr-hBN- $\chi_3$  AA vertical heterostructure, we have exploited the density functional theory (DFT). DFT calculations are carried out by Quantum Espresso (QE) software [29]. In the process of relaxation, the structure is relaxed until the forces acting on atoms become smaller than  $10^{-2}$  Ry/Bohr. After geometric optimization, the calculated interlayer distance between the Gr and hBN (hBN and  $\chi_3$  borophene) is 4.07 (4.18) Å. To eliminate the interactions between supercell images, a vacuum spacing of 17 Å has been adopted along the perpendicular direction to the structure (z). The generalized gradient approximation (GGA) of Perdew–Burke–Ernzerhof (PBE) is selected to approximate the electronic exchange and correlation. The cut-off energy of the wave function (charge density) is 70 (280) Ry. Also, numerical integrations in the Brillouin zone are evaluated with the Monkhorst-Pack mesh ( $14 \times 8 \times 1$ ).



**Fig. 3. Schematic showing of relaxed Gr-hBN- $\chi_3$ -AA supercell (a) top view and (b) side view. Red, green, and blue spheres show nitrogen, boron, and carbon atoms.**

Fig. 3 shows the geometry of the Gr-hBN- $\chi_3$ -AA vertical heterostructure after the relaxation process. In supercell, the number of boron, carbon, and nitrogen atoms is 64, 48, and 24, respectively. We calculated the binding energy of the heterostructure as  $E_b = [E_{HS} - E_{Gr} - E_{hBN} - E_{X_3}]$  to investigate the stability of the structure. In this formula,  $E_{HS}$ ,  $E_{Gr}$ ,  $E_{hBN}$ , and  $E_{X_3}$  are the total energy of the heterostructure, isolated layered Gr, hBN, and  $\chi_3$  borophene, respectively. The binding energy for the supercell is  $-0.0945$  eV. This negative value means that the structure is stable. This parameter for Gr-hBN- $\chi_3$ -AB (AB stack between Gr and hBN) is  $-0.1244$  eV [19]; therefore, Gr-hBN- $\chi_3$ -AA is less stable than Gr-hBN- $\chi_3$ -AB. An important parameter in vertical heterostructures is lattice mismatch [9]. The lattice mismatch between hBN and  $\chi_3$  borophene layers is calculated at 0.0366 (0.0373) in the X (Y) directions for Gr-hBN- $\chi_3$ -AA vertical heterostructure. Since these values are small, they have little effect on the electronic characteristics of the structure.

The DFT results in this section are a yardstick for constructing the TB model. In this regard, to find the dominant orbitals, we calculated the partial density of state (PDOS) of the Gr-hBN- $\chi_3$ -AA supercell, as shown in Fig. 4. These post-processing calculations are performed by the QE PROJWFC module [29]. Fig. 4(a) illustrates the PDOS of the S, Px, Py, and Pz orbitals of the boron atoms of  $\chi_3$  borophene. As we can see, the Py and Pz orbitals of the boron atoms of  $\chi_3$  borophene pick up around the Fermi energy level. The PDOS of the orbitals of boron (nitrogen) atoms in hBN are shown in Fig. 4(b) (Fig. 4(c)). The Pz orbitals of boron and nitrogen atoms have the highest DOS contribution around the Fermi level. Like the hBN layer, the Pz orbital of the carbon atoms

in Gr has higher DOS around  $E_F$  (Fig. 4(d)). Based on these calculations, we have employed these dominant orbitals in the TB model. Finally, Fig. 4(e) shows the PDOS of the S and P orbitals, and also the total PDOS of the whole supercell.

To find the conduction band minimum ( $\Delta E_c$ ) and the valence band maximum ( $\Delta E_v$ ) between Gr and hBN layers, we carried out orbital projection calculations that are shown in Fig. 5. Fig. 5(a) separates bands of the three layers: graphene (red), boron nitride (blue), and  $\chi_3$  borophene (green) in the Gr-hBN- $\chi_3$ -AA supercell. Similarly, Fig. 5(b) shows separate orbitals of the atoms of the three materials involved in the band structure. According to this figure, the most effective orbitals involved in the band structure, at the energy levels close to the Fermi energy, are the Pz orbitals of C atoms in graphene, the Pz orbitals of B and N atoms in boron nitride, and the Py and Pz orbitals of B atoms in  $\chi_3$  borophene. The point with the \* sign on the energy axis is the Dirac point of graphene (0.23 eV). Also,  $\Delta E_c$  ( $\Delta E_v$ ) between graphene and hBN is 3.26 (1.34) eV.

Moreover, we calculated the electron concentration function (ELF) to illustrate the chemical bonds of the Gr-hBN- $\chi_3$ -AA supercell (Fig. 6). Generally, the ELF value is in the range of 0-1. For  $0 < ELF \leq 0.5$ , the interatomic bonds are ionic; otherwise, those are considered covalent [30]. Figs. 6(a)-6(c) show the 2D ELF plots for the Gr, hBN, and  $\chi_3$  borophene layers, respectively. For Gr and hBN layers, each atom creates covalent bonds with its three neighboring atoms. For the  $\chi_3$  borophene layer, atoms with 4 (5) neighbors form strong covalent bonds with 3 (2) neighbors. The 2D ELF view of the supercell from the side view is shown in Fig. 6(d) so that vdW bonds between atoms in different layers are evident.

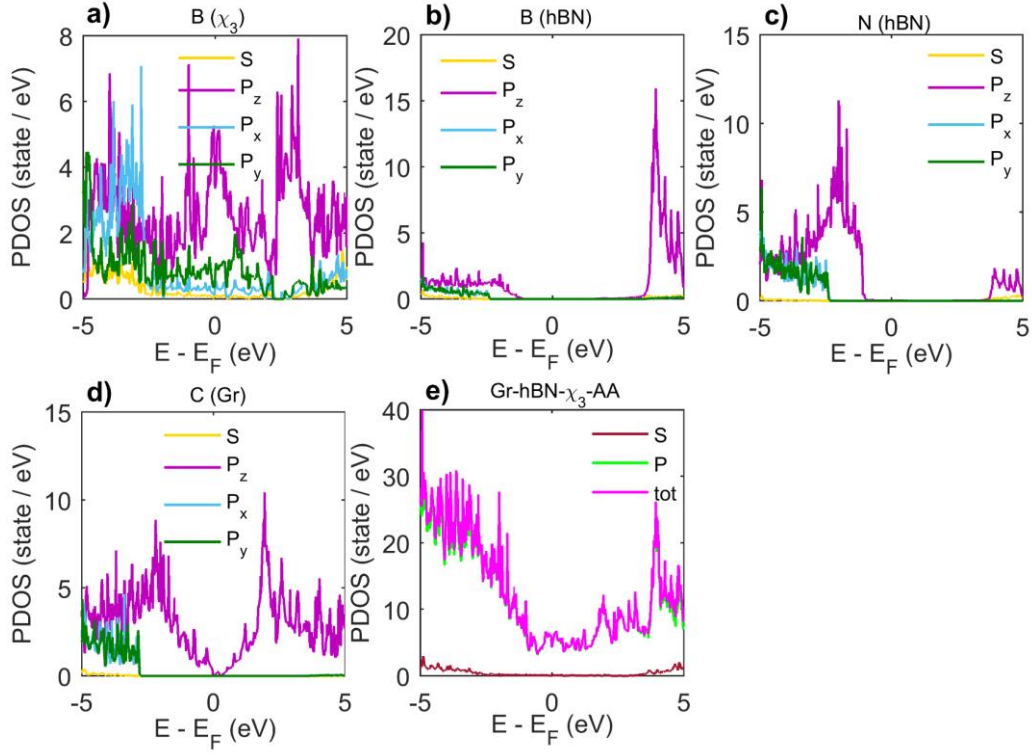


Fig. 4. PDOS for Gr-hBN- $\chi_3$ \_AA supercell. For orbitals of (a) B atoms in  $\chi_3$  borophene, (b) B, (c) N atoms in hBN layer, (d) C atoms in Gr, (e) S, P, and total PDOS of Supercell.

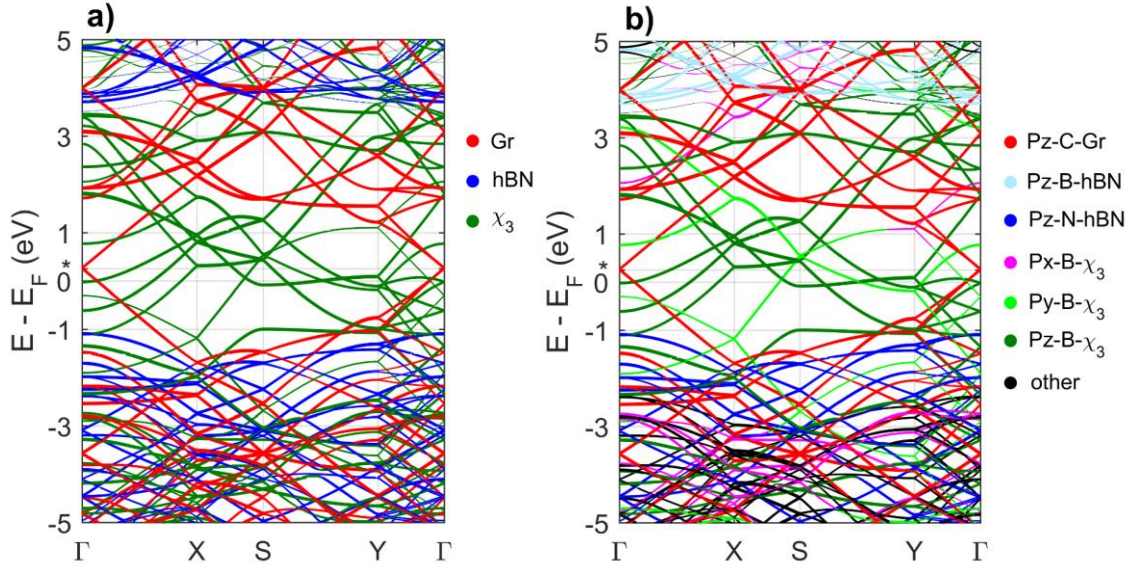


Fig. 5. Projection band structure (PBAND) for Gr-hBN- $\chi_3$ \_AA supercell. (a) Separate bands for three materials of the structure (b) separate orbitals of atoms of the three layers. The \* sign on the vertical axis corresponds to the Dirac point energy of graphene, which is 0.23 eV.



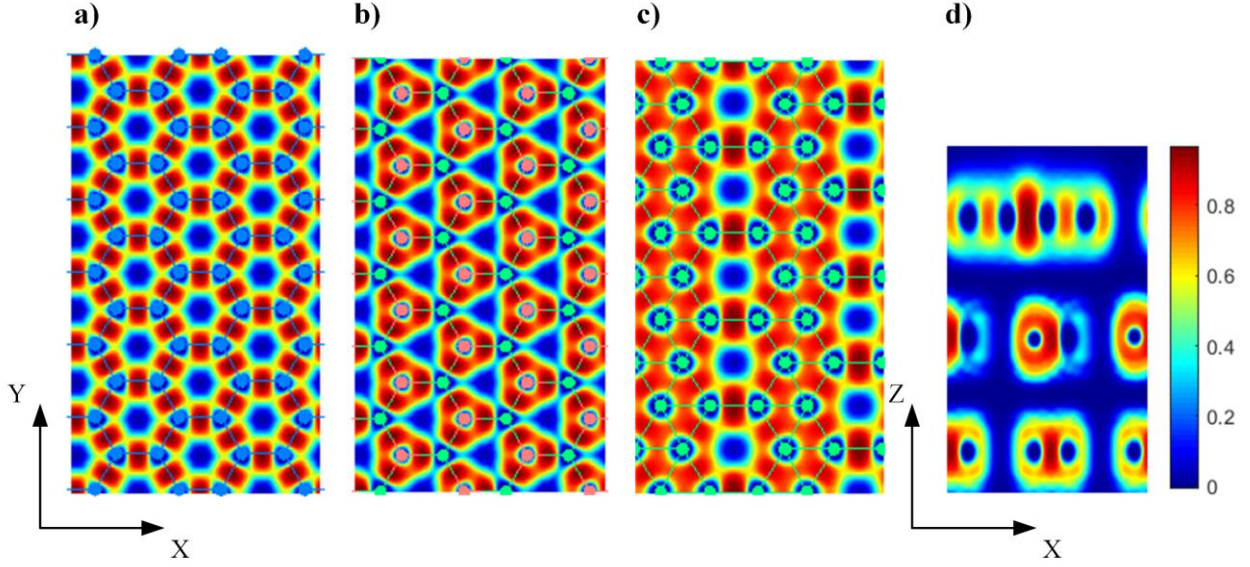


Fig. 6. (a) 2D-ELF profile form (a) bottom view (Gr), (b) hBN, (c) top view ( $\chi_3$  borophene). (d) side view of Gr-hBN- $\chi_3$ \_AA supercell. From the bottom, the first to third layers are graphene, boron nitride, and  $\chi_3$  borophene.

### B. Tight-Binding Modeling

The TB model is a popular method for calculating the band structure of solid-state systems [31]. Hamiltonian of the studied heterostructure is as follows:

$$[H] = [H_0] + \sum_{m=1}^4 [H_{nm}] \exp(i \vec{k} \cdot \vec{d}_m) \quad (1)$$

$[H_0]$  is the unit cell Hamiltonian, and  $[H_{nm}]$  is the interaction between the unit cell and the neighbor's  $m$ th unit cell.  $\vec{d}_m$  defines the vector that connects the unit cell to the  $m$ th neighbor.  $[H_0]$  in (1) is as follows:

$$[H_0] = \begin{pmatrix} H_{Gr} & \zeta_{Gr-hBN} & \\ \zeta_{Gr-hBN}^\dagger & H_{hBN} & \zeta_{hBN-\chi_3} \\ & \zeta_{hBN-\chi_3}^\dagger & H_{\chi_3} \end{pmatrix} \quad (2)$$

In (2),  $H_{\chi_3}$  and  $H_{Gr}$  are hopping between boron and carbon atoms on the  $\chi_3$  and Gr sheets, respectively.  $H_{hBN}$  describes a Hamiltonian matrix of the hBN layer. Out-plane hopping between carbon atoms in the graphene layer and boron and nitrogen atoms in the hBN layer is described by  $\zeta_{Gr-hBN}$ . Similarly,  $\zeta_{hBN-\chi_3}$  depicts out-plane hopping between boron and nitrogen atoms in the hBN layer and boron atoms in the  $\chi_3$  borophene layer. All relevant hopping parameters are described based on Slater-Koster (SK) parameters [31].

To find the out-plane hopping between  $\chi_3$  and hBN layers, i.e.,  $\zeta_{hBN-\chi_3}$ , we consider the interlayer hopping of the  $i$ th B

atom in the  $\chi_3$  layer and the  $j$ th B or N atom in the hBN layer [32] as

$$h_{P_z(B)/P_z(B)}(i, j) = \left[ n_{i,j}^2 (V_{pp\sigma}^{B,B}) + (1 - n_{i,j}^2) (V_{pp\pi}^{B,B}) \right] \times \exp\left(-\frac{r_{i,j}}{P}\right)^\xi \quad (3)$$

$$h_{P_z(B)/P_z(N)}(i, j) = \left[ n_{i,j}^2 (V_{pp\sigma}^{B,N}) + (1 - n_{i,j}^2) (V_{pp\pi}^{B,N}) \right] \times \exp\left(-\frac{r_{i,j}}{P}\right)^\xi \quad (4)$$

The cosine of the angle between the vector that points  $j$ th B or N atom to  $i$ th B atom and the  $z$ -axis, represented by  $n_{i,j}$ . Also,  $r_{i,j}$  shows the distance between the  $i$ th B atom and the  $j$ th B or N atom.  $\zeta$  and  $P$  parameters provide one degree of freedom for a better fit. We consider that the base orbitals are orthonormal; therefore, the overlap matrix is unitary. The SK parameters of the structure are described in Table 1.

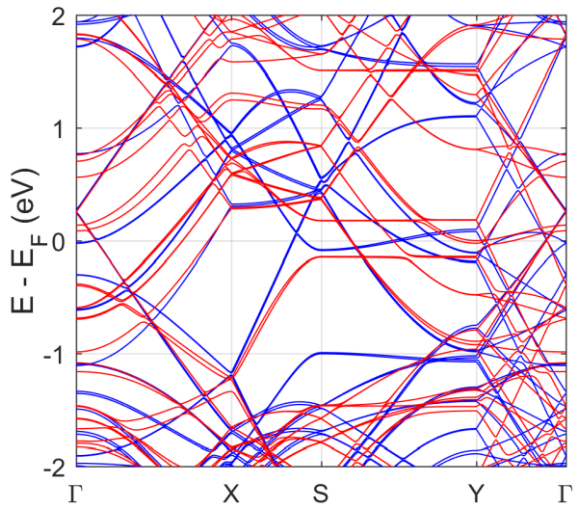
To fit the DFT and TB band structures, we apply the least-squares method [33]. Data of DFT and TB band structures are specified by  $E_j^{DFT}$  and  $E_j^{TB}$ , which represents the  $j$  band at  $k$  point. The error function is defined as a weighted sum as follows:

$$S(p) = \sum_j \frac{[E_j^{DFT} - E_j^{TB}]^2}{\sigma_j^2} \quad (5)$$

**Table 1. SK Parameters of the device.**

Parameters	Onsite	Bond	Layer
$V_{pp\sigma}^{\chi_3}$	...	B-B	$\chi_3$
$V_{pp\pi}^{\chi_3}$	...	B-B	$\chi_3$
$V_{pp\pi}^{hBN}$	...	B-N	hBN
$V_{pp\pi}^{Gr}$	...	C-C	Gr
$V_{pp\sigma}^{B,B}$	...	B-B (vertical)	$\chi_3$ & hBN
$V_{pp\pi}^{B,B}$	...	B-B (vertical)	$\chi_3$ & hBN
$V_{pp\sigma}^{B,N}$	...	B-N (vertical)	$\chi_3$ & hBN
$V_{pp\pi}^{B,N}$	...	B-N (vertical)	$\chi_3$ & hBN
$V_{pp\sigma}^{B,C}$	...	B-C (vertical)	hBN & Gr
$V_{pp\sigma}^{N,C}$	...	N-C (vertical)	hBN & Gr
$\Delta_{p_y}^{\chi_3}$	Py_B	...	$\chi_3$
$\Delta_{p_z}^{\chi_3}$	Pz_B	...	$\chi_3$
$\Delta_{p_z(B)}^{hBN}$	Pz_B	...	hBN
$\Delta_{p_z(N)}^{hBN}$	Pz_N	...	hBN
$\Delta_{p_z}^{Gr}$	Pz_C	...	Gr

Where  $\sigma_j$  and  $p$  are the weight of the error function and TB parameters, respectively. To obtain the optimal SK parameters, function  $S$  is minimized with respect to  $p$ . The best TB parameters are presented in Table 2. Fig. 7 compares DFT and TB band structures.

**Fig. 7. Comparison of DFT and TB band structures**

### C. NEGF Technique

Fig. 8(a) and (b) show the side and top views of the device, respectively, in nanoribbon mode (VTGNR  $\chi_3$  NRFET) and width  $w=1.477$  nm. Also, we have considered the length of the device to be 0.85 nm. The orange color characterizes the channel area. Semi-infinite leads are considered at the ends of the bottom graphene sheet and the top  $\chi_3$  borophene sheet, utilizing the self-energy definition. This work presents the Hamiltonian in real space mode [34]. In this work, neither the source nor the drain electrodes are doped, and scattering effects have been neglected during calculation.

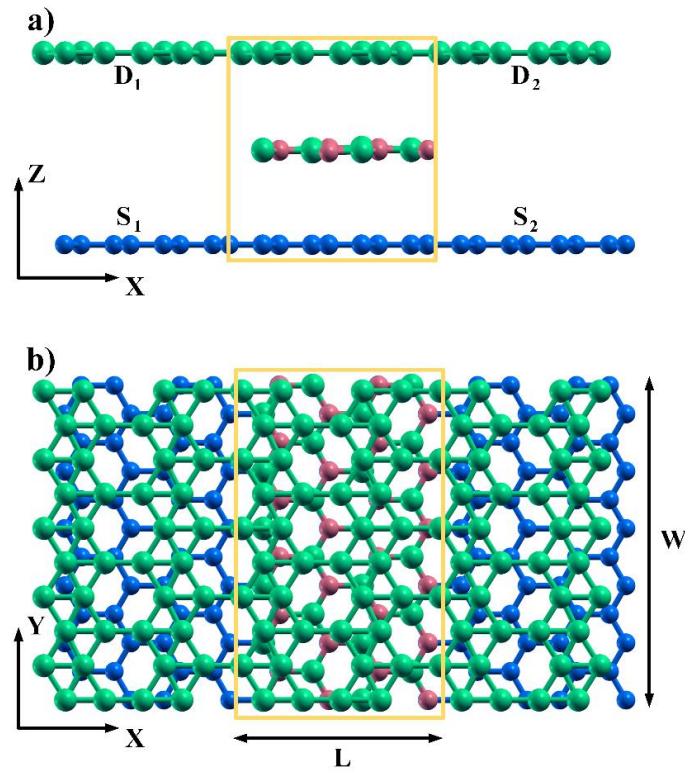
The retarded Green's function with four contacts, the transmission function, current, and total current between  $j$  and  $k$  contacts of the device, are represented in Eqs. 6, 7, 8, and 9, respectively [35, 36].

$$G(E) = \left[ EI - H - \sum_{S_1}(E) - \sum_{S_2}(E) - \sum_{D_1}(E) - \sum_{D_2}(E) \right]^{-1} \quad (6)$$

$$T_{jk}(E) = \sum_{k_y} \text{Trace} \left[ \Gamma_j(E) G(E) \Gamma_k(E) G^\dagger(E) \right] \quad (7)$$

**Table 2. TB parameters Gr-hBN- $\chi_3$ \_AA.**

Parameter	Value	Parameter	Value
$V_{pp\sigma}^{\chi_3}$	3.075 (eV)	$V_{pp\sigma}^{B,B}$	0.1 (eV)
$V_{pp\pi}^{\chi_3}$	-1.65 (eV)	$V_{pp\pi}^{B,B}$	-0.055 (eV)
$\Delta_{p_y}^{\chi_3}$	2.53 (eV)	$V_{pp\sigma}^{B,N}$	0.11 (eV)
$\Delta_{p_z}^{\chi_3}$	1.2 (eV)	$V_{pp\pi}^{B,N}$	-0.04 (eV)
$V_{pp\pi}^{hBN}$	2.58 (eV)	$V_{pp\sigma}^{B,C}$	0.12 (eV)
$\Delta_{p_z(B)}^{hBN}$	3.5124 (eV)	$V_{pp\sigma}^{N,C}$	0.06 (eV)
$\Delta_{p_z(N)}^{hBN}$	-1.0849 (eV)	$\xi$	0
$V_{pp\pi}^{Gr}$	2.53 (eV)	$P$	1 (Å)
$\Delta_{p_z}^{Gr}$	0.2517 (eV)		



**Fig. 8. Schematic of channel, and source and drain contacts of VTGNR $\chi_3$ NRFET and width  $W=1.477$  nm (a) Side (b) Top view.**

$$I_{jk} = \frac{2q}{h} \int T_{jk}(E) (f_j(E) - f_k(E)) dE \quad (8)$$

$$I = \sum_{j,k} I_{j,k} \quad (9)$$

Where  $\sum_{S_1, S_2}$  and  $\sum_{D_1, D_2}$  are self-energies of the source and drain contacts, so that  $j = S_1, S_2$  and  $k = D_1, D_2$ , and  $\Gamma(E) = i [\sum(E) - \sum(E)^\dagger]$  is the broadening function.

Fig. 9 shows the equivalent capacitive circuit model for the device. This model has been used to calculate the potential of barrier layers.  $C_{ox}$  and  $C_t$  are the gate oxide ( $\text{SiO}_2$ ) and the tunneling barrier (hBN) capacitors, respectively. These two capacitors are calculated by Eq. 10, where  $t_{ox}$  and  $t_{hBN}$  are the thickness of  $\text{SiO}_2$  and hBN, respectively.  $C_{QS}$  ( $C_{QD}$ ) is the quantum capacitor of graphene (borophene) sheets, which is calculated using Eq. 11 [37]. We assumed  $E_{FS} = 0$ , and the Fermi level of the drain is  $E_{FD} = E_{FS} - qV_B$ . The energies of the source and drain Dirac points are  $-qV_S$  and  $-qV_D$ , respectively. Also, it is assumed that the potential along the hBN layers changes linearly. To calculate the potential in the channel potential, the capacitive circuit model of Fig. 9 should be analyzed self-consistent with (11).

$$C_{ox} = \epsilon_{ox} / t_{ox}, \quad C_t = \epsilon_{hBN} / t_{hBN} \quad (10)$$

$$C_Q(V_{ch}) = q^2 \int_{-\infty}^{\infty} DOS(E) \frac{\text{sech}^2(E - qV_{ch} / 2KT)}{4KT} dE \quad (11)$$

#### 4- Results

As shown in Fig. 8, the hBN layer has been sandwiched between graphene and  $\chi_3$  borophene in the device, with four contacts. In 2D mode, the width of the nanoribbon is also

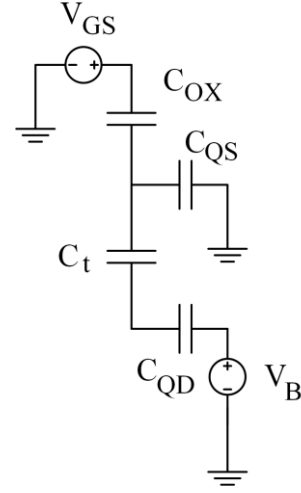


Fig. 9. Equivalent capacitive circuit model for the device.

repeated with period  $W$  in the  $Y$  direction. In calculations,  $t_{ox}$  is assumed to be 1nm.

Fig. 10(a) illustrates the transmission coefficient in terms of energy for the device and three different widths. According to the figure, as the width of the nanoribbon decreases, the energy gap ( $E_g$ ) of the graphene nanoribbon (GNR) increases. Therefore, the transmission coefficient of the carrier decreases. The steep slope of the transmission coefficient around the Dirac point energy of graphene (0.23 eV) indicates the  $E_g$  of graphene. Also, for the width of 1.477 nm, it can be seen that the edge of the hBN conduction band is at the energy of 3.49 eV, and the edge of the hBN valence band is at the energy of -1.11 eV. For energies larger than the conduction band edge and lower than the valence band edge, the transmission probability is due to thermionic emission.

Fig. 10(b) illustrates the current density of VTGNR $\chi_3$ NRNRFET at a width of 1.477 nm in terms of drain-source voltage for different gate-source voltages. As can be seen, in a  $V_{DS} > 0$ , the current is low (high) at  $V_{GS} (-V_{GS})$ , and

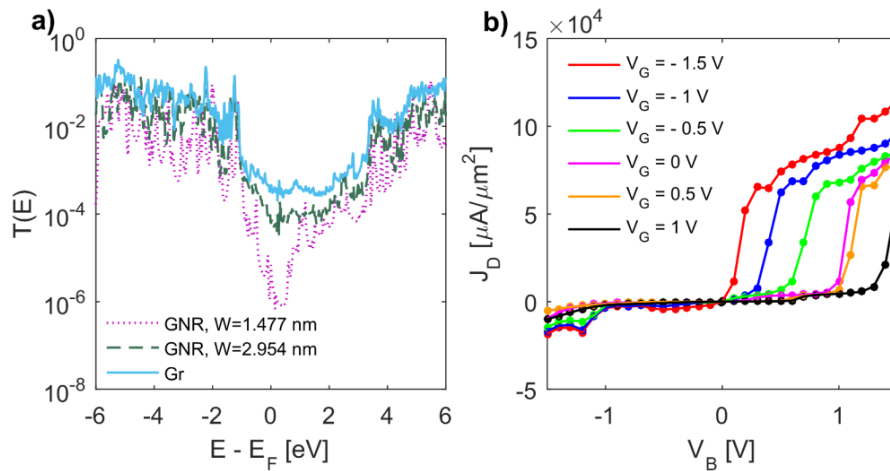


Fig. 10. (a) Transmission coefficient of VTGNR $\chi_3$ NRNRFET for different nanoribbon widths compared to VTGr $\chi_3$ 3FET (b) Drain current density in terms of drain-source voltage for VTGNR $\chi_3$ NRNRFET width  $W = 1.477$  nm.



**Table 3. FOM of VTGr $\chi_3$ FETs.**

Device	$I_{ON}/I_{OFF}$	$SS_{min}$ (mv/dec)	$\tau$ (ps)	$ V_{DS} $	$ V_{GS} $
VTGNR $\chi_3$ NRFET, W=1.477 nm	186	256	0.011	0.5	1.5
VTGNR $\chi_3$ NRFET, W=2.954 nm	3.14	1115	0.5	0.5	1.5
VTGr $\chi_3$ FET, 2D	3.12	2014	2.858	0.5	1.5

**Table 4. Comparison of parameters of the considered device with other related works.**

References	Structure	$t_{barrier}$ (nm)	$SS_{min}$ (mv/dec)	$(I_{ON}/I_{OFF})_{max}$
Brittenl et al. [11]	Gr-hBN-Gr	...	...	50
Yu et al. [16]	Gr-MoS <sub>2</sub> -Ti	~15	...	$10^3$
Liu et al. [18]	Gr-MoS <sub>2</sub> -Ag	0.65	...	26
Abbasi et al. [19]	GNR-hBN- $\chi_3$ -AB	0.829	343	113
This work	GNR-hBN- $\chi_3$ -AA	0.824	256	186

the transistor is in the OFF (ON) state.

Switching ratio ( $I_{ON}/I_{OFF}$ ), subthreshold swing ( $SS$ ) [34], and gate-delay time ( $\tau$ ) [38] are important characteristics of the device defined as:

$$SS = \frac{dV_G}{d(\log(I_D))} \quad (12)$$

$$\tau = \frac{Q_{ON} - Q_{OFF}}{I_{ON}} \quad (13)$$

$$Q = -e \int LDOS(E) f(E - E_F) dE + e \int LDOS(E) (1 - f(E - E_F)) dE \quad (14)$$

Where  $Q_{ON}$  and  $Q_{OFF}$  are the total charges of the device in the source and drain regions, at ON and OFF states, respectively, and LDOS is the local density of states [34].

Table 3 shows the figure of merit (FOM) of VTGr $\chi_3$  FET. As can be seen from Table 3, the  $I_{ON}/I_{OFF}$  ratio of the transistor increases with the decrease in the width of the GNR. Because with the decrease in the width of GNR, the  $E_g$  of GNR increases, and as a result, the OFF current decreases, therefore  $I_{ON}/I_{OFF}$  increases. Also, the decrease in the ribbon's width improves  $SS$ . Because it leads to weaker quantum effects

(decreasing density of state and quantum capacitances), and it makes the control of the gate on the channel better. Moreover,  $\tau$  improves with decreasing the width of GNR.

Table 4 compares the parameters of the considered device and other related works (metallic drain). As can be seen from Table 4, the thickness of the tunneling barrier plays an essential role in improving the  $I_{ON}/I_{OFF}$ . Also, changing the stack type between Gr and hBN layers has little effect on the FOM of the device [19]. To improve the performance of VTFET, it is recommended to use materials in the source and drain with an energy gap, and also in the tunneling barrier with a smaller energy gap [39]. Moreover, a combination of lateral and vertical structures has the potential to improve the performance of VTFET.

## 5- Conclusion

This work uses DFT theory to investigate the electronic properties (PDOS, PBAND, and ELF) of Gr-hBN- $\chi_3$ -AA vertical heterostructure. We concluded that the Gr-hBN- $\chi_3$ -AA is less stable than Gr-hBN- $\chi_3$ -AB. Also, the NEGF technique, along with the TB model, has been applied to calculate the electrical characteristics of the considered device. The results show that decreasing the width of the device improves parameters  $I_{ON}/I_{OFF}$ ,  $SS$ , and  $\tau$ . The device permits a gate-delay time of 0.011 ps at room temperature. The results show that changing the stack between Gr and hBN layers has little effect on the device's FOM. Also, a combination of lateral and vertical structures with a suitable design can improve the performance of VTFET.

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## Data availability

All data that support the findings of this study are included in the article.

## Conflict of Interest

The authors declare that they have no conflict of interest.

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