

# *Explanation of Warp Knitted Fatigue Behavior under the Cyclic Extension by using Holloman's Relation*

Mir Reza Taheri Otaghsara<sup>i</sup>; Ali A.A. Jeddi<sup>ii</sup>; Jamshid Aghazadeh Mohandesi<sup>iii</sup>

## **ABSTRACT**

In this study, tensile and fatigue behavior of seven different structure (Tricot, Locknit, reverse Locknit, three needle Satin, four needle Satin, three needle Sharkskin and four needle Sharkskin) of warp knitted fabrics with three different course density (cpc) have been studied. The correlation between tensile and <sup>iv</sup>fatigue behavior of these fabrics with structural parameters have been investigated. The space of yarn movement and the length of underlaps are taken into consideration as basic parameters influencing the corresponding mechanical behavior. The obtained results show that with the increase in underlap length and/or cpc, the breaking extension percent is decreased while the breaking tenacity is increased. Cyclic extension causes stress relaxation and strain softening in the warp knitted fabrics. Application of Holloman's relation ( $\sigma=K \varepsilon^n$ ) to the results of tensile and fatigue tests shows that strength coefficient (K) is decreased by fatigue process, while strain-hardening coefficient (n) is increased. By increasing underlap length, the cyclic stabilized load and strain-hardening coefficient is increased. Also, the cyclic stabilized load and the strain-hardening coefficient in fabrics with longer back guide bar underlap is higher than those with the same length in front guide bar.

## **KEYWORDS**

Fabric fatigue, Warp knitted fabrics, Tensile property, Fatigue property, Cyclic extension, Strain hardening, Holloman's relation

## **1. INTRODUCTION**

Fatigue of textile materials has been investigated by many researchers [1-8]. Prevorsek and Lyons [1,2] have studied the fatigue behavior of textile fibers. In these studies, fatigue life under constant total extension (stroke), rather than stress amplitude has been taken as a more practical method for the case of single fiber specimens. In a general introduction to a series of investigation [3], a brief consideration was given to the distribution of individual lifetime of an acrylic sample at a given frequency and stroke. Lyons [4] have studied the effect of

frequency of cyclic loading on fatigue endurance of acrylic fibers and presented the equation  $N = a \nu^{-n}$  where N is the number of cycle that fibers withstand under cyclic loading,  $\nu$  is the frequency, a is a function of stroke, and n is a constant  $>0$ . Lyons [9-13] and Lyons and Ribnik [14] have shown that the stroke and frequency of cyclic loading, temperature, molecule structure and molecule weight of fibers effect on the fatigue behavior of fibers. They observed stress decrement and non-recoverable extension during each cycle

which are functions of stress relaxation and creep extension. Narisava et al. [15] investigated the fatigue behavior of nylons at fixed extension strokes and the growth

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of specimen was not taken up. They observed that stress amplitude gradually decreased to a stationary value with increasing number of fatigue cycles.

Frank and Singleton [6] showed that plasticizers in the form of heat and/or water tend to increase the fatigue life of filament yarns. They observed that durability of nylon, polyester and viscoseryon yarns against cyclic deformation depending on the frequency of cyclic straining, temperature, humidity of ambient differed each other and depend on the structure and physical properties (regain and thermoplastic property) of these yarns. Jeddi et al. [7] have investigated the tensile fatigue behavior of cotton-polyester blended spun yarns. They concluded that yarn decrimping, fiber slippage and fiber elongation are the factors that influence fatigue endurance of the yarn, and the polyester component in the blended yarn causes significant improvement of damping ability and the fatiguing resistance of the yarn under the tensile cyclic loading.

Few papers have concentrated on the fatigue behavior of textile fabrics. Kobliakov et al. [8] reported limited experimental results on tensile fatigue behavior of woven and knitted fabrics under different frequencies of cyclic straining and stroke. They found that by increasing the frequency of cyclic loading the fabrics deformation (i.e., the ratio of non-recoverable elongation to the initial length of specimen) decreases, however with the increase in the stroke, the deformation increases, they also showed that this deformation for knitted fabrics is higher than woven fabrics, and weft knitted fabrics reach the final deformation limit earlier than the woven fabrics. Jeddi et al. [16] have designed a machine for fatiguing the warp knitted fabrics. They knitted fabrics (i.e., Tricot, Locknit, Reverse Locknit, Satin and Sharkskin) and investigated the relationship between fatigue behavior of fabrics and their structural parameters. They observed that the phenomenon of fabrics fatigue under cyclic tension depend on the geometry of fabric structure, and the final deformation and tensile modulus of the fabrics increased as the number of fatigue cycles increased, while tensile breaking extension% decreased. Ben Abdessalem et al. [17] have developed a new experimental device permitting to test dimensional behaviors of knitted fabrics under large number of cyclic elongation. They observed that the fatigue test applied to a plain knitted fabric made of cotton involved a variation fabrics dimensions and a permanent deformation that persists after relaxation and this permanent deformation depends widely on the number of repetitive cycles. Also, they concluded that the deformation involved by fatigue test corresponds to a displacement and a lengthening of the yarn composing the loop.

In the present study, two fully threaded guide bars warp knitted fabrics were produced from polyester textured filament yarn count 11.2 tex (100 denier). The objects of this investigation are the study of tensile behavior of these fabrics and the effects of fabric structures, course density (cpc) and amplitude of cyclic extension on their fatigue behavior and to obtain the cyclic stabilized load of fabrics in different amplitude of extension. Then, we use Holloman's relation to obtain the strain-hardening coefficient and strength coefficient to assess the behavior of fabrics after fatiguing.

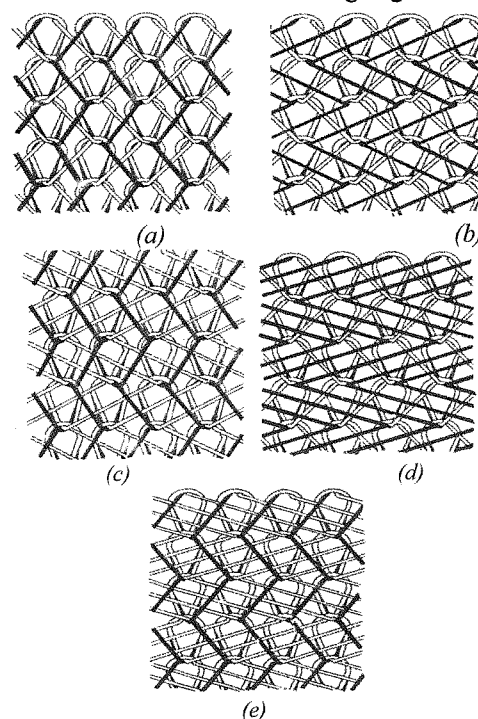


Figure 1: Double guide bar warp knitted fabrics. (a) Tricot; (b) Locknit; (c) Reverse Locknit; (d) Three needle Satin; (e) Three needle Sharkskin.

## 2. MATERIAL AND METHODS

The fabric samples were made on a Karl Mayer Ketten KH<sub>2</sub> machine, with gauge 28 (28 needle per inch). These fabrics are Tricot, Locknit, Reverse Locknit, three needle Satin, four needle Satin, three needle Sharkskin and four needle Sharkskin, and each of them knitted in three different course density setting (15, 20, and 25 cpc). Figure 1 shows five fabric structures. After knitting process, all the fabrics were washed to remove spin finish and industrial oil contaminants and then heat set. After heat setting the cpc of fabrics were slightly changed. The characteristics of fabrics are shown in Table 1.

### A. Tensile Tests

To study the tensile properties of the fabrics and in order to

obtain the parameters of cyclic tests, fabric samples were tested on a servo-hydraulic **Instron 8502** testing machine. Considering high load capacity ( $\pm 500\text{kN}$ ) of the testing machine, in order to increase the accuracy of measurements, the specimens of 50cm width were 8 folded for tensile tests. Five specimens with 50mm gauge length for each fabric were tested in course direction. The reason for choosing 50 mm gauge length is the limitation of the movement course of the moving clamp. Two typical load-extension diagrams ( $T_2$  and  $SHF_3$ ) are demonstrated in Figure 2.

TABLE 1  
CHARACTERISTICS OF KNITTED FABRICS.

Fabric Structure (No. of underlap) FB* BB*	Fabric code	Run-in (cm)		Fabric density ( $\text{cm}^{-1}$ )	
		FB	BB	cpc*	wpc*
1 Tricot 1	$T_1$	163.3	153	20.2	12.1
	$T_2$	142.7	138.7	23	13.5
	$T_3$	135.7	127	25.2	14.7
2 Locknit 1	$L_1$	208	156.4	18	14.8
	$L_2$	190	135	21.1	15.9
	$L_3$	176.7	126	23.1	16.8
1 Reverse Locknit 2	$RL_1$	168.5	196	18.1	13.1
	$RL_2$	153	177.5	21.7	13.8
	$RL_3$	143.4	168.7	25.2	13.7
3 Satin 3 1	$ST_1$	250.5	155	16.8	15.8
	$ST_2$	231	127	20.5	16.5
	$ST_3$	216	121.5	22.7	16.8
4 Satin 4 1	$SF_1$	289	155	16.4	16.2
	$SF_2$	271.5	129	20.5	16.9
	$SF_3$	259.4	22.4	23	16.8
1 Sharkskin 3 3	$SHT_1$	171.5	234.5	17.5	13.1
	$SHT_2$	153	221.5	21.7	13.7
	$SHT_3$	150	207.1	23.5	13.7
1 Sharkskin 4 4	$SHF_1$	170.5	279	17.7	13
	$SHF_2$	148	274.5	21.3	2.6
	$SHF_3$	148	267.5	22.6	12.5

FB: front guide bar; BB: back guide bar; cpc: course per cm; wpc: wale per cm.

As shown in Figure 2, the diagram of load-extension of all fabrics has two slopes, and then the specimen will break. The angle of second slope is wider and slopes are separated by a knee which is taken into consideration as a criterion for obtaining the amplitude of cyclic extension in fatigue test.

### B. Fatigue Tests

After cycling a material for a relatively short duration, the hysteresis loops generally stabilizes and the material achieves equilibrium condition for imposed strain limits.

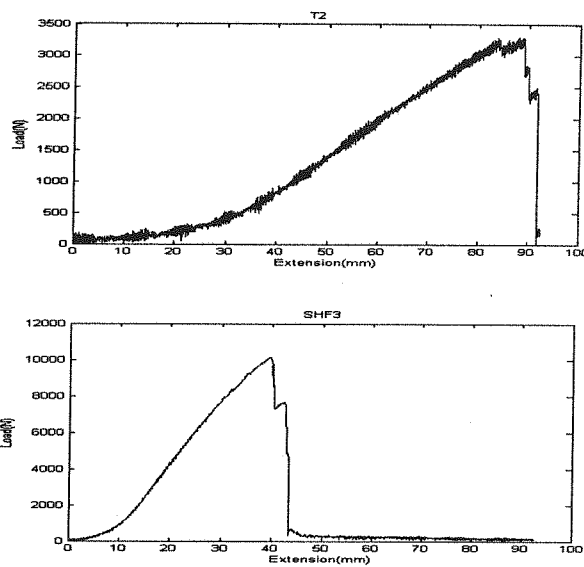


Figure 2: Typical load – extension diagrams of  $T_2$  and  $SHF_3$  samples.

The cyclic stress-strain response of the material may then be quite different from the initial monotonic response. Cyclically stress-strain curves are important characterizations of a material's cyclic response. These curves may be obtained in several methods [18]: 1. A series of companion samples may be cycled within various strain limits until the respective hysteresis loops become stabilized. The cyclic stress-strain curve is then determined by fitting a curve through the tips of the various superimposed hysteresis loop. 2. A faster method for obtaining cyclic stress-strain curves is by multiple step testing, wherein the same sample is subjected to a series of alternating strains of increasing magnitude. In this manner, one specimen yields several hysteresis loops, which may be used to construct the stress-strain curve. 3. An even quicker technique involving only one sample has been found to provide excellent results and is used extensively in current cyclic strain testing experiments. In this manner, the specimen is subjected to a series of blocks of gradually increasing and then decreasing strain excursion. In the present study, the first method was used to achieve more accuracy in the tests.

The specimens for the purpose of fatigue tests were prepared as mentioned for tensile tests and all fatigue tests were carried out under a preload of 500 N. This preload causes an extension which is settled down in the second slope of load-extension diagram for all fabric samples. The amplitude of cycling were 2,4,6,8,10 and 12mm, were chosen from the elongation of fabrics in order to conduct cycling in the second slope region of load-extension diagram of fabrics samples. For each abovementioned amplitude of extension one sample has been tested.

In this study, the FLAPS software (Fatigue Life Analysis Programs) has been applied to run the tests and data acquisition. The frequency of cycling was set at 0.5 Hz, and

data sampling rate was set at 2 Hz. Each sample has been tested during 500 cycles.

Load-strain curves have been used instead of stress-strain curve to assess the effects of fatigue loading on the fabrics. To obtain the cyclic load-strain curve, a computer program was written by using MATLAB software to obtain the cyclic stabilized load in each fatigue test. The maximum load for first cycle in each test has taken as monotonic load for given amplitude to draw the monotonic load-strain curves.

### 3. RESULTS AND DISCUSSIONS

The amplitude of slippage and movement of components of materials over each other owing to tension or compression are the important factors that influence the elastic behavior of materials. Therefore, when a filament yarn is subjected to a tensile load, its strain depends on the ability of the movement of molecule chain on each other. This phenomenon, in fabrics depends not only on the nature of the yarn used in fabric, but also on the structural properties of the fabric. It means that the strain and ability of fabrics to withstand against a given load depend on the slippage and movement of yarns in the fabric structure. In warp knitted fabrics, the following two structural parameters have significant role in fabric elasticity [16]:

1) **The space for yarn movement;** this space allows yarn movement over each other inside the fabric structure. In double guide bar warp knitted fabrics, this space is formed between overlaps and front guide bar underlap and the movement of back guide bar underlap depends on the extent of this space. If this space is large enough, the back guide bar underlap can move easily.

2) **The length of underlaps;** with increase in the length of front and/or back guide bar underlap length, then the strain value in the course direction will be decreased while in the wale direction it will increased.

The existing space for yarn movement plays the main role in elastic behavior of warp knitted fabric rather than the length of underlap. Very often these two parameters have an opposite influence on fabric elasticity.

#### A. Tensile Properties

The average results of tensile test of fabrics are shown in Table 2. Statistical examination at 95% confidence limit has applied to the tensile results. Table 3 shows the results of ANOVA test. This table shows that Duncan statistical test can be used for breaking extension and breaking tenacity grouping. Table 4 shows the grouping for breaking extension and breaking tenacity of studied fabric structures in different cpc levels. As shown in Table 4, the breaking extension and the breaking tenacity of all fabric structures with different cpc are settled nearly in three

distinguished group except breaking extension of Locknit structure (L).

TABLE 2  
THE AVERAGE RESULTS OF TENSILE TESTS.

Fabric code	Breaking Extension (mm)	Breaking Tenacity (N)
T <sub>1</sub>	85.4	3072
T <sub>2</sub>	83.59	3277
T <sub>3</sub>	81.86	3509
L <sub>1</sub>	73.75	3142
L <sub>2</sub>	72.11	3344
L <sub>3</sub>	71.54	3898
RL <sub>1</sub>	75.16	3635
RL <sub>2</sub>	65.66	4710
RL <sub>3</sub>	56.79	5743
ST <sub>1</sub>	59.5	3968
ST <sub>2</sub>	57.2	4154
ST <sub>3</sub>	55.3	4323
SF <sub>1</sub>	57.3	5873
SF <sub>2</sub>	54.51	6278
SF <sub>3</sub>	51.47	6636
SHT <sub>1</sub>	53.28	5340
SHT <sub>2</sub>	46.8	7075
SHT <sub>3</sub>	42.33	7767
SHF <sub>1</sub>	46.1	7956
SHF <sub>2</sub>	38.78	9643
SHF <sub>3</sub>	37.24	10350

Figure 3 shows graphically the average breaking elongation results of the fabrics in tensile tests. The beaking elongation in fabrics with longer back guide bar underlap is lower than those with the same length of underlap in front guide bar (RL<L, SHF<SF and SHT<ST). This is because of the shorter length of front guide bar under lap than back

TABLE 3  
ANOVA TEST ON THE TENSILE PROPERTIES AT 95% CONFIDENCE LIMIT.

Structure	Breaking Extension		Breaking Tenacity	
	F	Sig.	F	Sig.
T	7.214	0.009	19.37	0.000
L	1.802	0.207	36.01	0.000
RL	79.763	0.000	313.3	0.000
ST	5.690	0.018	6.126	0.015
SF	6.600	0.012	34.07	0.000
SHT	25.586	0.000	315.0	0.000
SHF	22.525	0.000	380.2	0.000

guide bar underlap and then less accessible space for back guide bar underlap in fabrics RL, SHT, and SHF. This smaller space causes limited yarn movement in these fabrics. With the increase of cpc and number of underlap the breaking elongation is decreased. These phenomena are because of the

closer angle between underlaps and direction of tensile load in fabrics with higher course density (cpc) and/or more number of underlaps. For this reason, the yarn movement and thereafter the fabric elongation is limited.

TABLE 4

DUNCAN GROUPING ARRANGEMENT FOR BREAKING EXTENSION AND BREAKING TENACITY.

Structure	cpc	Breaking Extension Group			Breaking Tenacity Group		
		1	2	3	1	2	3
T	Level 1	85.4			3072		
	Level 2	83.6	83.6			3277	
	Level 3		82.0				3509
L	Level 1	71.5			3142		
	Level 2	72.1				3344	
	Level 3	73.8					3898
RL	Level 1	75.3			3635		
	Level 2		65.7			4710	
	Level 3			56.8			5743
ST	Level 1	59.5			3968		
	Level 2	57.2	57.2		4154	4154	
	Level 3		55.3			4323	
SF	Level 1	57.3			5873		
	Level 2	54.5	54.5			6278	
	Level 3		51.5				6638
SHT	Level 1	53.3			5340		
	Level 2		46.8			7075	
	Level 3			42.3			7767
SHF	Level 1	46.1			7956		
	Level 2		38.8			9643	
	Level 3		37.2				10350

Figure 4 shows the breaking tenacity of fabrics. This figure shows that the breaking tenacity of fabrics with longer back guide bar underlap is higher than fabrics with the same length in front guide bar underlap. This phenomenon can be explained as existing of less space for the movement of back guide bar underlap in those fabrics. Also, Figure 4 shows that with the increase of cpc the breaking tenacity of fabrics is increased. The main reason of this result is the existence of more courses in the samples of higher cpc.

### B. Fatigue Properties

Figure 5 shows typical diagram of load-extension and load-time for T<sub>1</sub> and SHF<sub>2</sub> samples in cyclic test. As illustrated in this figure, the maximum load gradually decreases in subsequent cycles and there is a hysteresis loop that the width of this loop also decreases gradually. The trend of variation of maximum load shows that this load will reach to a constant amount as cyclically stabilized load and fabric samples achieve the equilibrium condition for the corresponding imposed strain. The main parameters of cyclic tests and maximum load at first cycle and stabilized state of fabrics are tabulated in Table 5.

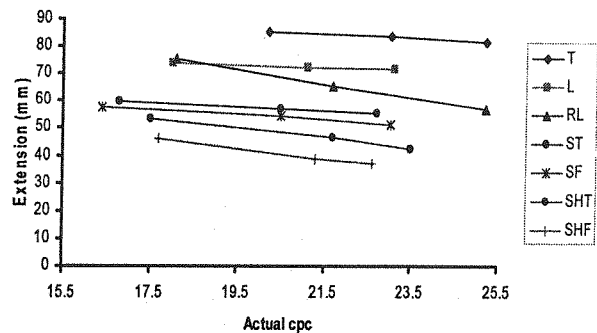


Figure 3: Breaking elongation of fabrics in different actual cpc.

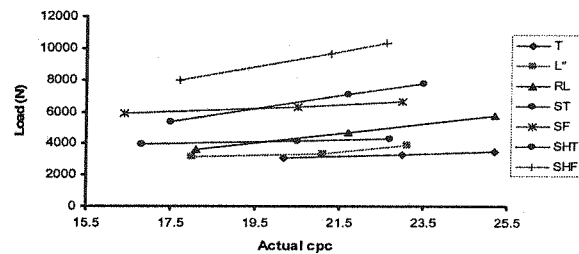


Figure 4: Breaking tenacity of fabrics in different actual cpc.

The maximum load in first cycle and the maximum load in stabilized state have registered for comparing behaviors of fabrics before and after fatigue process (Table 5). Figure 6 shows typical regression diagram of monotonic and cyclically stabilized load-strain curves for two fabric structures of Tricot and four needles Sharkskin with nominal cpc 15. By comparing the monotonic and cyclically stabilized load-strain curves (Figure 6), it can be seen that cyclic stabilized load-strain curve is placed under the monotonic load-strain curve. This indicates that, fatigue process causes strain softening in fabrics. These observation can be explained by stress relaxation of yarn in fabric structure [1,4,6,7,16] and the deformation of loop shape[17].

Figure 7 shows a typical cyclic stabilized load- amplitude regression curve for Locknit (L) and three needle Sharkskin (SHT) structures with different cpc. It can be seen that by increasing cpc, the cyclic stabilized load of fabrics is increased. The main reason for this phenomenon is the presence of more courses in specimen and the higher friction between yarns, in the structures with higher cpc.

The regression curve for cyclic stabilized load of all fabric structures with nominal cpc 20 in different amplitude of cycling is shown in Figure 8. This figure shows that by

TABLE 5

PARAMETERS OF TESTS AND MAXIMUM LOADS AT FIRST CYCLE AND AT STABILIZED STATE IN FATIGUE TESTS.

Sample code	PE (mm)	AC (mm)	ML (N)	SL (N)	Sample code	PE (mm)	AC (mm)	ML (N)	SL (N)	Sample code	PE (mm)	AC (mm)	ML (N)	SL (N)
T <sub>1</sub>	47.05	2	546	312	T <sub>2</sub>	33.34	2	548	390	T <sub>3</sub>	29.76	2	590	394
T <sub>1</sub>	43.97	4	780	450	T <sub>2</sub>	32.36	4	896	582	T <sub>3</sub>	26.62	4	772	516
T <sub>1</sub>	44.65	6	994	583	T <sub>2</sub>	33.97	6	1082	718	T <sub>3</sub>	28.41	6	1008	701
T <sub>1</sub>	43.95	8	1200	732	T <sub>2</sub>	33.85	8	1290	873	T <sub>3</sub>	25.85	8	1270	893
T <sub>1</sub>	44.11	10	1460	902	T <sub>2</sub>	31.27	10	1670	1099	T <sub>3</sub>	26.5	10	1536	1127
T <sub>1</sub>	44.15	12	1550	936	T <sub>2</sub>	34.26	12	2104	1500	T <sub>3</sub>	29.04	12	1854	1290
L <sub>1</sub>	36.6	2	538	357	L <sub>2</sub>	32.02	2	666	456	L <sub>3</sub>	25.9	2	762	476
L <sub>1</sub>	33.8	4	708	447	L <sub>2</sub>	29.25	4	758	528	L <sub>3</sub>	26.81	4	1082	718
L <sub>1</sub>	33.6	6	952	592	L <sub>2</sub>	26.62	6	1032	658	L <sub>3</sub>	23.04	6	1402	922
L <sub>1</sub>	35.8	8	1172	749	L <sub>2</sub>	28.95	8	1370	919	L <sub>3</sub>	26.53	8	1900	1318
L <sub>1</sub>	35.15	10	1444	937	L <sub>2</sub>	30.14	10	1730	1176	L <sub>3</sub>	25.27	10	2306	1564
L <sub>1</sub>	36.15	12	1742	1149	L <sub>2</sub>	27.67	12	2028	1425	L <sub>3</sub>	21.93	12	2532	1751
RL <sub>1</sub>	25.68	2	642	374	RL <sub>2</sub>	20.27	2	704	447	RL <sub>3</sub>	16.89	2	868	527
RL <sub>1</sub>	27.19	4	852	549	RL <sub>2</sub>	18.48	4	1100	660	RL <sub>3</sub>	14.44	4	1318	877
RL <sub>1</sub>	25.57	6	1132	670	RL <sub>2</sub>	20.7	6	1536	993	RL <sub>3</sub>	15.33	6	1960	1456
RL <sub>1</sub>	25.35	8	1395	838	RL <sub>2</sub>	21.22	8	1906	1287	RL <sub>3</sub>	15.6	8	2600	1850
RL <sub>1</sub>	25.1	10	1606	1071	RL <sub>2</sub>	19.81	10	2282	1492	RL <sub>3</sub>	14.92	10	3172	2249
RL <sub>1</sub>	25.15	12	1890	1266	RL <sub>2</sub>	21.17	12	2674	1841	RL <sub>3</sub>	13.41	12	3686	2573
ST <sub>1</sub>	33.4	2	720	350	ST <sub>2</sub>	23.55	2	686	421	ST <sub>3</sub>	21.09	2	920	554
ST <sub>1</sub>	34.79	4	1036	558	ST <sub>2</sub>	24.03	4	1036	671	ST <sub>3</sub>	19.68	4	1224	820
ST <sub>1</sub>	32.73	6	1356	788	ST <sub>2</sub>	25.16	6	1520	967	ST <sub>3</sub>	20.62	6	1722	1158
ST <sub>1</sub>	30.16	8	1930	1152	ST <sub>2</sub>	22.13	8	2398	1594	ST <sub>3</sub>	20.51	8	2454	1604
ST <sub>1</sub>	29.34	10	2498	1560	ST <sub>2</sub>	21.14	10	3322	2267	ST <sub>3</sub>	19.27	10	3210	2204
ST <sub>1</sub>	30.48	12	2888	1890	ST <sub>2</sub>	22.19	12	3620	2501	ST <sub>3</sub>	20.02	12	3990	2813
SF <sub>1</sub>	27.18	2	726	394	SF <sub>2</sub>	20.69	2	834	548	SF <sub>3</sub>	19.12	2	978	596
SF <sub>1</sub>	26.19	4	1176	631	SF <sub>2</sub>	19.61	4	1194	750	SF <sub>3</sub>	22.17	4	1792	1090
SF <sub>1</sub>	26.04	6	1746	978	SF <sub>2</sub>	20.01	6	2314	1471	SF <sub>3</sub>	18.9	6	2620	1697
SF <sub>1</sub>	25.93	8	2330	1572	SF <sub>2</sub>	20.65	8	3250	2180	SF <sub>3</sub>	19.86	8	4178	2818
SF <sub>1</sub>	25.88	10	2960	1837	SF <sub>2</sub>	20.49	10	3788	2629	SF <sub>3</sub>	21.66	10	4868	3222
SF <sub>1</sub>	25.16	12	3878	2484	SF <sub>2</sub>	18.55	12	2518	3625	SF <sub>3</sub>	18.4	12	5130	3533
SHT <sub>1</sub>	20.07	2	880	456	SHT <sub>2</sub>	11.23	2	912	582	SHT <sub>3</sub>	10.87	2	1328	888
SHT <sub>1</sub>	20.26	4	1528	809	SHT <sub>2</sub>	11.93	4	1774	1153	SHT <sub>3</sub>	9.58	4	2164	1446
SHT <sub>1</sub>	19.37	6	2096	1258	SHT <sub>2</sub>	11.44	6	2680	1621	SHT <sub>3</sub>	11.69	6	3498	2386
SHT <sub>1</sub>	18.79	8	2532	1610	SHT <sub>2</sub>	12.48	8	4168	2873	SHT <sub>3</sub>	10.06	8	4410	3072
SHT <sub>1</sub>	18.04	10	3778	2122	SHT <sub>2</sub>	10.82	10	4704	3321	SHT <sub>3</sub>	9.46	10	5390	3857
SHT <sub>1</sub>	19	12	3776	2529	SHT <sub>2</sub>	10.79	12	4956	3426	SHT <sub>3</sub>	9.17	12	6344	4542
SHF <sub>1</sub>	12.6	2	978	609	SHF <sub>2</sub>	6.62	2	1172	729	SHF <sub>3</sub>	7.31	2	1172	714
SHF <sub>1</sub>	11.68	4	1970	1155	SHF <sub>2</sub>	7.78	4	2025	1326	SHF <sub>3</sub>	7.02	4	2600	1656
SHF <sub>1</sub>	12.2	6	3296	2124	SHF <sub>2</sub>	6.8	6	4022	2797	SHF <sub>3</sub>	6.32	6	4220	2929
SHF <sub>1</sub>	11.27	8	4306	2916	SHF <sub>2</sub>	6.59	8	5608	4037	SHF <sub>3</sub>	6.63	8	5660	3987
SHF <sub>1</sub>	11	10	5586	3824	SHF <sub>2</sub>	6.86	10	6580	4705	SHF <sub>3</sub>	6.76	10	7094	4990
SHF <sub>1</sub>	10.95	12	6436	4448	SHF <sub>2</sub>	7.56	12	8578	6750	SHF <sub>3</sub>	6.61	12	8342	5787

PE: Pre-extension of fabric for 500N preload; AC: amplitude of cycling; ML: maximum load at first cycle; SL: maximum load at stabilization.

increasing the number of underlaps the cyclic stabilized load is increased (SF<sub>2</sub>>ST<sub>2</sub>>L<sub>2</sub>>T<sub>2</sub> and SHF<sub>2</sub>>SHT<sub>2</sub>>RL<sub>2</sub>>T<sub>2</sub>). This is due to the closer angle between longer underlap and load direction, and subsequently lower contribution of yarn movement in fabric deformation. Also, the cyclically stabilized load of fabrics with longer underlap in back guide bar is higher than those with the same underlap length in front guide bar (RL<sub>2</sub>>L<sub>2</sub>, SHT<sub>2</sub>>ST<sub>2</sub> and SHF<sub>2</sub>>SF<sub>2</sub>). It can be attributed to the number of contact points between back guide bar underlap with legs of loops. The number of contact points for Tricot, Locknit, reverse Locknit, three and four needle

Sharkskin are 1, 3, 5, and 7, respectively (refer to Figure 1).

### C. Holloman's Mathematical Description of Fabric Fatigue

From the Holloman's relation given by  $\sigma = K \epsilon^n$ , it is possible to mathematically describe the material load-strain response in either the monotonic or cyclically stabilized state. Consequently strain-hardening coefficient for both monotonic ( $n_1$ ) and cyclic ( $n_2$ ) conditions and the strength coefficient for both monotonic ( $K_1$ ) and cyclic ( $K_2$ ) conditions can be calculated. The strain-hardening

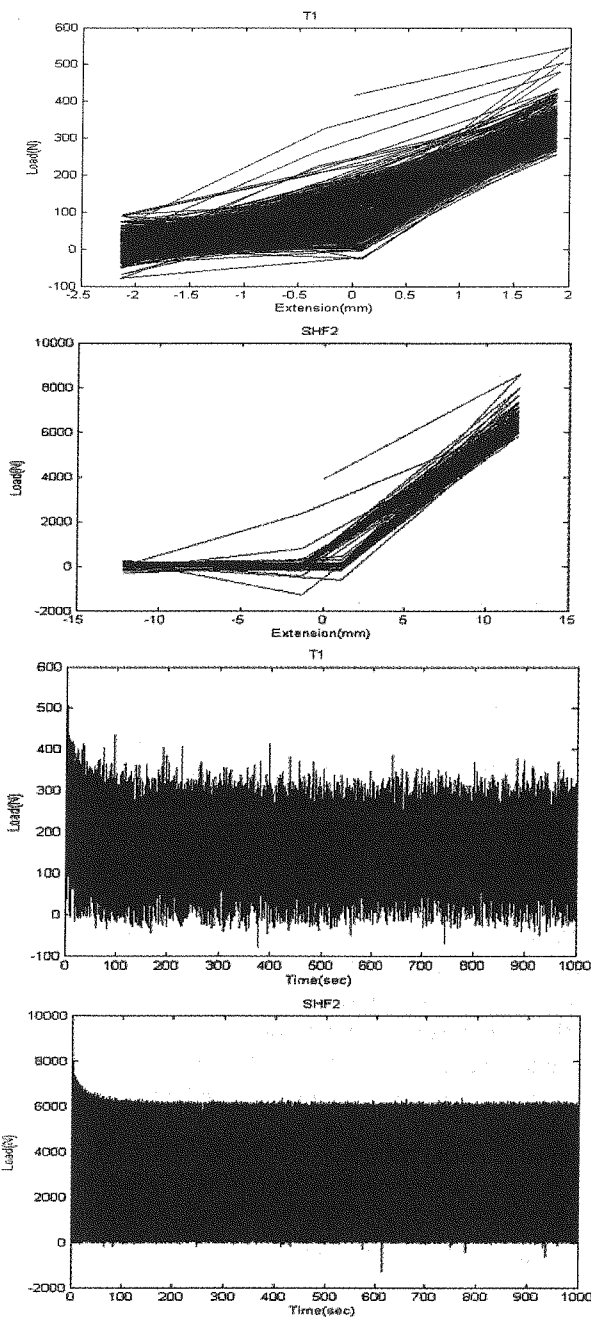


Figure 5: Typical diagrams of load-extension and load-number of cycle of samples  $T_1$  ( $AC=2mm$ ) and  $SHF_2$  ( $AC=12mm$ ).

coefficients and strength coefficients of all fabric structures in monotonic and cyclic stabilized conditions are shown in Table 6.

As it can be seen from Table 6, in all fabric structures  $K_1 > K_2$ , it means that cyclic extension causes strain softening in all fabrics. This is due to stress relaxation in fabrics during cyclic extension. Conversely, we can see that in all fabric structures  $n_2 > n_1$ , it means that after cyclic loading the elastic property of samples are increased. This is because of the decreasing angle between underlaps and the load direction, and then decreasing the contribution of yarn movement after fatigue process. Also,

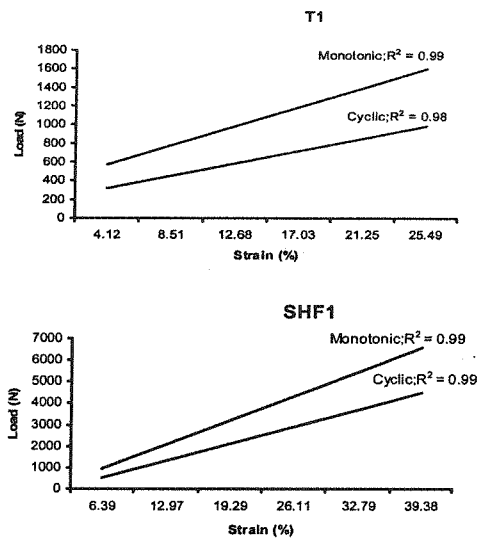


Figure 6: Monotonic and cyclic load-strain regression curves for  $T_1$  and  $SHF_1$  samples.

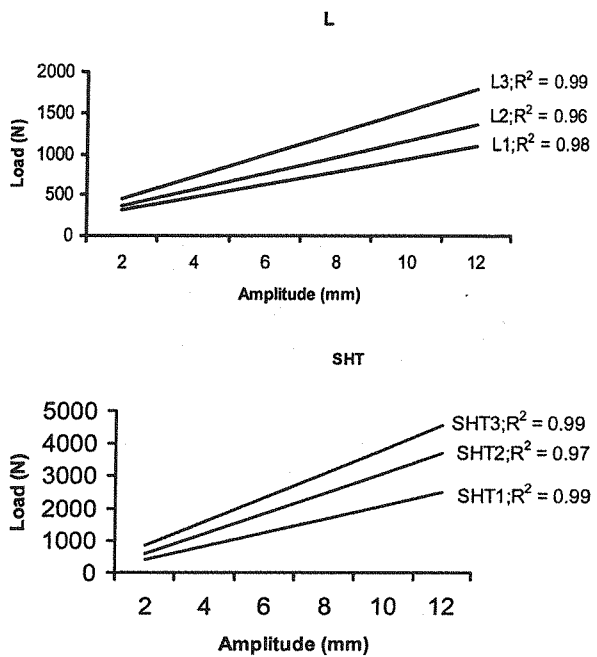


Figure 7: The regression for cyclic stabilized load of fabrics with different cpc at different amplitude of cycling.

during fatigue process, the higher molecular orientation of yarn in fabric structure causes higher elastic property of fabrics.

Figure 9 shows the strain-hardening coefficient of fabrics with different structures. The trend shows that with the increase of underlap length the strain-hardening coefficient of fabrics is increased. This is because of the lower angle between longer underlaps and direction of force and orientation of molecule chain in the yarns. Also, the strain-hardening coefficient in fabrics with longer underlap in back guide bar is higher than those in front guide bar. The explanation of this phenomenon is the same

as section 3.B

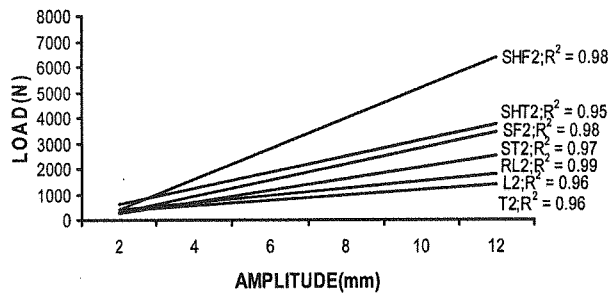


Figure 8: Regression for cyclic stabilized load of fabrics with different structure with nominal cpc 20 at different amplitude of cycling.

TABLE 6  
STRENGTH COEFFICIENT AND STRAIN-HARDENING COEFFICIENT OF FABRICS WITH DIFFERENT CPC.

Fabric code	$K_1$	$K_2$	$n_1$	$n_2$
T <sub>1</sub>	271.1	148.4	0.516	0.558
T <sub>2</sub>	251.4	155.9	0.596	0.607
T <sub>3</sub>	235.9	150.6	0.561	0.591
L <sub>1</sub>	220.8	143.3	0.579	0.575
L <sub>2</sub>	253.7	173.5	0.566	0.562
L <sub>3</sub>	292.5	177.4	0.598	0.633
RL <sub>1</sub>	264	145.9	0.542	0.562
RL <sub>2</sub>	249.5	148.4	0.645	0.677
RL <sub>3</sub>	250.7	188.72	0.71	0.719
ST <sub>1</sub>	266.5	121.3	0.659	0.748
ST <sub>2</sub>	238.7	125.2	0.723	0.802
ST <sub>3</sub>	282.3	167	0.691	0.732
SF <sub>1</sub>	242.4	123.4	0.74	0.798
SF <sub>2</sub>	237.8	150.1	0.805	0.824
SF <sub>3</sub>	313.4	165	0.775	0.838
SHT <sub>1</sub>	313.6	145.6	0.667	0.758
SHT <sub>2</sub>	269.4	167.1	0.782	0.809
SHT <sub>3</sub>	399.9	258.1	0.721	0.745
SHF <sub>1</sub>	285.9	168.8	0.813	0.847
SHF <sub>2</sub>	288.7	178.5	0.853	0.889
SHF <sub>3</sub>	323.3	195.2	0.832	0.869

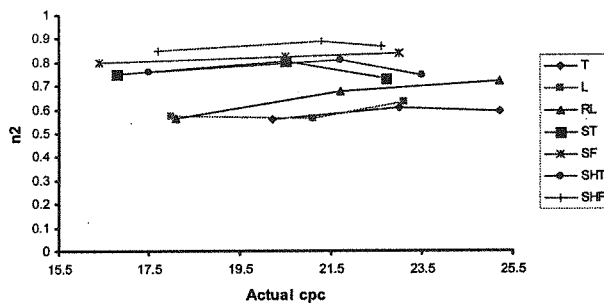


Figure 9: Strain-hardening coefficient of fabrics with different structures.

#### 4. CONCLUSION

In this study, tensile and fatigue behavior of several structures of warp knitted fabrics with three different cpc

have investigated. It was shown that the fatigue properties of warp knitted fabrics depend on the structure of fabrics. It seems that the mechanism of the fatigue failure of these fabrics and the cyclic stabilized load can be controlled by the structural parameters of these fabrics, i.e.,: a) The movement space of yarn in fabric structure, and b) the length of underlaps.

The breaking strain of fabrics decreases with the increase of underlap length, while breaking tenacity will increase, and breaking strain in fabrics with longer underlap in front guide bars is more than fabrics with the same length of underlaps in back guide bars conversely, the breaking tenacity of fabrics with longer underlap in back guide bar is more than the fabrics with the same length in front guide bar.

Cyclic extension causes stress relaxation in warp knitted fabrics and the maximum load in each cycle decreases as the number of cycle is increased and the maximum load reaches to a constant amount as cyclic stabilized load. The results show that the cyclic extension causes strain softening in all fabrics.

To assess mathematically the behavior of fabrics before and after cyclic loading, the Holloman's relation ( $\sigma = K \epsilon^n$ ) has been applied. The results show that in all fabrics, the strength coefficient decreased after cyclic loading ( $K_1 > K_2$ ) and conversely, the strain-hardening coefficient is increased ( $n_2 > n_1$ ). Comparison of fabrics with different structure shows that, by increasing the underlap length, the strain-hardening coefficient is increased, also the strain-hardening coefficient of fabrics with longer underlap in back guide bar is higher than the fabrics of the same length of underlap in front guide bar. Therefore, it can be concluded that the Holloman's relation is a good approach to explain the fatigue behavior of warp knitted fabrics.

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